

**M317 Assignment #5 due Friday**

For each of the following limits, use the definition of function limit to find an L such that  $\lim_{x \rightarrow c} f(x) = L$  and prove it (i.e., find  $\delta(\varepsilon)$  or  $B(\varepsilon)$  )

1.  $\lim_{x \rightarrow 2} \frac{x^2 - x - 2}{x^2 + 2x - 8}$

2.  $\lim_{x \rightarrow 1} \frac{x}{x + 1}$

3.  $\lim_{x \rightarrow 0} \frac{1 - \cos(x)}{x}$

4.  $\lim_{x \rightarrow \infty} \frac{\cos(x)}{x^2}$

5.  $\lim_{x \rightarrow \infty} \frac{x}{1 + x^2}$

Use the sequential definition of function limit to show the following limits fail to exist

6.  $\lim_{x \rightarrow 0} \cos\left(\frac{1}{x}\right)$

7.  $\lim_{x \rightarrow 0} f(x)$  where  $f(x) = \begin{cases} 2 & \text{if } x > 2 \\ -2 & \text{if } x < 2 \end{cases}$